# CHAPTER 12

Selecting a Sample

# In this chapter you will learn about:

- The differences between sampling in qualitative and quantitative research
- Definitions of sampling terminology
- The theoretical basis for sampling
- Factors affecting the inferences drawn from a sample
- Different types of sampling including:
  - Random/probability sampling designs
  - Non-random/non-probability sampling designs
  - The 'mixed' sampling design
- The calculation of sample size
- The concept of saturation point

**Keywords:** accidental sampling, cluster sampling, data saturation point, disproportionate sampling, equal and independent, estimate, information-rich, judgemental sampling, multi-stage cluster sampling, non-random sample, population mean, population parameters, quota sampling, random numbers, random sample, sample statistics, sampling, sampling design, sampling element, sampling error, sampling frame, sampling population, sampling unit, sample size, sampling strategy, saturation point, snowball sampling, study population, stratified sampling, systematic sampling.

## The differences between sampling in quantitative and qualitative research

The selection of a sample in quantitative and qualitative research is guided by two opposing philosophies. In quantitative research you attempt to select a sample in such a way that it is unbiased and represents the population from where it is selected. In qualitative research, number considerations

may influence the selection of a sample such as: the ease in accessing the potential respondents; your judgement that the person has extensive knowledge about an episode, an event or a situation of interest to you; how typical the case is of a category of individuals or simply that it is totally different from the others. You make every effort to select either a case that is similar to the rest of the group or the one which is totally different. Such considerations are not acceptable in quantitative research.

The purpose of sampling in quantitative research is to draw inferences about the group from which you have selected the sample, whereas in qualitative research it is designed either to gain in-depth knowledge about a situation/event/episode or to know as much as possible about different aspects of an individual on the assumption that the individual is typical of the group and hence will provide insight into the group.

Similarly, the determination of sample size in quantitative and qualitative research is based upon the two different philosophies. In quantitative research you are guided by a predetermined sample size that is based upon a number of other considerations in addition to the resources available. However, in qualitative research you do not have a predetermined sample size but during the data collection phase you wait to reach a point of data saturation. When you are not getting new information or it is negligible, it is assumed you have reached a data saturation point and you stop collecting additional information.

Considerable importance is placed on the sample size in quantitative research, depending upon the type of study and the possible use of the findings. Studies which are designed to formulate policies, to test associations or relationships, or to establish impact assessments place a considerable emphasis on large sample size. This is based upon the principle that a larger sample size will ensure the inclusion of people with diverse backgrounds, thus making the sample representative of the study population. The sample size in qualitative research does not play any significant role as the purpose is to study only one or a few cases in order to identify the spread of diversity and not its magnitude. In such situations the data saturation stage during data collection determines the sample size.

In quantitative research, randomisation is used to avoid bias in the selection of a sample and is selected in such a way that it represents the study population. In qualitative research no such attempt is made in selecting a sample. You purposely select 'information-rich' respondents who will provide you with the information you need. In quantitative research, this is considered a biased sample.

Most of the sampling strategies, including some non-probability ones, described in this chapter can be used when undertaking a quantitative study provided it meets the requirements. However, when conducting a qualitative study only the non-probability sampling designs can be used.



FIGURE 12.1 The concept of sampling

# The concept of sampling

Let us take a very simple example to explain the concept of sampling. Suppose you want to estimate the average age of the students in your class. There are two ways of doing this. The first method is to contact all students in the class, find out their ages, add them up and then divide this by the number of students (the procedure for calculating an average). The second method is to select a few students from the class, ask them their ages, add them up and then divide by the number of students you have asked. From this you can make an *estimate* of the average age of the class. Similarly, suppose you want to find out the average income of families living in a city. Imagine the amount of effort and resources required to go to every family in the city to find out their income! You could instead select a few families to become the basis of your enquiry and then, from what you have found out from the few families, make an estimate of the average income of families in the city. Similarly, election opinion polls can be used. These are based upon a very small group of people who are questioned about their voting preferences and, on the basis of these results, a *prediction* is made about the probable outcome of an election.

**Sampling**, therefore, is the process of selecting a few (a sample) from a bigger group (the **sampling population**) to become the basis for estimating or predicting the prevalence of an unknown piece of information, situation or outcome regarding the bigger group. A sample is a subgroup of the population you are interested in. See Figure 12.1.

This process of selecting a sample from the total population has advantages and disadvantages. The advantages are that it saves time as well as financial and human resources. However, the disadvantage is that you *do not find out the information* about the population's characteristics of interest to you but *only estimate* or *predict* them. Hence, the possibility of an error in your estimation exists.

Sampling, therefore, is a trade-off between certain benefits and disadvantages. While on the one hand you save time and resources, on the other hand you may compromise the level of accuracy in your findings. Through sampling you only make an estimate about the actual situation prevalent in the total population from which the sample is drawn. If you ascertain a piece of information from the total sampling population, and if your method of enquiry is correct, your findings should be reasonably accurate. However, if you select a sample and use this as the basis from which to estimate the situation in the total population, an error is possible. Tolerance of this possibility of error is an important consideration in selecting a sample.

## Sampling terminology

Let us, again, consider the examples used above where our main aims are to find out the average age of the class, the average income of the families living in the city and the likely election outcome for a particular state or country. Let us assume that you adopt the sampling method – that is, you select a few students, families or electorates to achieve these aims. In this process there are a number of aspects:

- The class, families living in the city or electorates from which you select you select your sample are called the *population* or **study population**, and are usually denoted by the letter *N*.
- The small group of students, families or electors from whom you collect the required information to estimate the average age of the class, average income or the election outcome is called the **sample**.

- The number of students, families or electors from whom you obtain the required information is called the **sample size** and is usually denoted by the letter *n*.
- The way you select students, families or electors is called the **sampling design** or **sampling strategy**.
- Each student, family or elector that becomes the basis for selecting your sample is called the **sampling unit** or **sampling element**.
- A list identifying each student, family or elector in the study population is called the **sampling frame**. If all elements in a sampling population cannot be individually identified, you cannot have a sampling frame for that study population.
- Your findings based on the information obtained from your respondents (sample) are called **sample statistics.** Your sample statistics become the basis of estimating the prevalence of the above characteristics in the study population.
- Your main aim is to find answers to your research questions in the study population, not in the sample you collected information from. From sample statistics we make an estimate of the answers to our research questions in the study population. The estimates arrived at from sample statistics are called *population parameters* or the **population mean**.

# **Principles of sampling**

The theory of sampling is guided by three principles. To effectively explain these, we will take an extremely simple example. Suppose there are four individuals A, B, C and D. Further suppose that A is 18 years of age, B is 20, C is 23 and D is 25. As you know their ages, you can *find out* (calculate) their average age by simply adding 18 + 20 + 23 + 25 = 86 and dividing by 4. This gives the average (mean) age of A, B, C and D as 21.5 years.

Now let us suppose that you want to select a sample of two individuals to make an *estimate* of the average age of the four individuals. To select an unbiased sample, we need to make sure that each unit has an equal and independent chance of selection in the sample. **Randomisation** is a process that enables you to achieve this. In order to achieve randomisation we use the theory of probability in forming pairs which will provide us with six possible combinations of two: A and B; A and C; A and D; B and C; B and D; and C and D. Let us take each of these pairs to calculate the average age of the sample:

- 1. A + B = 18 + 20 = 38/2 = 19.0 years;
- 2. A + C = 18 + 23 = 41/2 = 20.5 years;
- 3. A + D = 18 + 25 = 43/2 = 21.5 years;
- 4. B + C = 20 + 23 = 43/2 = 21.5 years;
- 5. B + D = 20 + 25 = 45/2 = 22.5 years;
- 6. C + D = 23 + 25 = 48/2 = 24.0 years.

Notice that in most cases the average age calculated on the basis of these samples of two (sample statistics) is different. Now compare these sample statistics with the average of all four individuals – the population mean (population parameter) of 21.5 years. Out of a total of six possible sample combinations, only in the case of two is there no difference between the sample statistics and the population mean. Where there is a difference, this is attributed to the sample and is known as **sampling error**. Again, the size of the sampling error varies markedly. Let us consider the difference in the sample statistics and the population mean for each of the six samples (Table 12.1).

TABLE 12.1 The difference between sample statistics and the population mean

Sample	Sample average (sample statistics) (1)	Population mean (population parameter) (2)	Difference between (1) and (2)	
1	19.0	21.5	-2.5	
2	20.5	21.5	-1.5	
3	21.5	21.5	0.0	
4	21.5	21.5	0.0	
5	22.5	21.5	+1.0	
6	24.0	21.5	+2.5	

This analysis suggests a very important principle of sampling:

**Principle 1** – in a majority of cases of sampling there will be a difference between the sample statistics and the true population mean, which is attributable to the selection of the units in the sample.

To understand the second principle, let us continue with the above example, but instead of a sample of two individuals we take a sample of three. There are four possible combinations of three that can be drawn:

1 A + B + C = 18 + 20 + 23 = 61/3 = 20.33 years;
 2 A + B + D = 18 + 20 + 25 = 63/3 = 21.00 years;
 3 A + C + D = 18 + 23 + 25 = 66/3 = 22.00 years;
 4 B + C + D = 20 + 23 + 25 = 68/3 = 22.67 years.

Now, let us compare the difference between the sample statistics and the population mean (Table 12.2).

	Sample average	Population average	Difference between
Sample	(1)	(2)	(1) and (2)
1	20.33	21.5	-1.17
2	21.00	21.5	-0.5
3	22.00	21.5	+0.5
4	22.67	21.5	+1.17

 TABLE 12.2
 The difference between a sample and a population average

Compare the differences calculated in Table 12.1 and Table 12.2. In Table 12.1 the difference between the sample statistics and the population mean lies between -2.5 and +2.5 years, whereas in the second it is between -1.17 and +1.17 years. The gap between the sample statistics and the population mean is reduced in Table 12.2. This reduction is attributed to the increase in the sample size. This, therefore, leads to the second principle:

**Principle 2** – the greater the sample size, the more accurate the estimate of the true population mean.

The third principle of sampling is particularly important as a number of sampling strategies, such as stratified and cluster sampling, are based on it. To understand this principle, let us continue with the same example but use slightly different data. Suppose the ages of four individuals are markedly different: A = 18, B = 26, C = 32 and D = 40. In other words, we are visualising a population where the individuals with respect to age – the variable we are interested in – are markedly different.

Let us follow the same procedure, selecting samples of two individuals at a time and then three. If we work through the same procedures (described above) we will find that the difference in the average age in the case of samples of two ranges between -7.00 and +7.00 years and in the case of the sample of three ranges between -3.67 and +3.67. In both cases the range of the difference is greater than previously calculated. This is attributable to the greater difference in the ages of the four individuals – the sampling population. In other words, the sampling population is more heterogeneous (varied or diverse) in regard to age.

**Principle 3** – the greater the difference in the variable under study in a population for a given sample size, the greater the difference between the sample statistics and the true population mean.

These principles are crucial to keep in mind when you are determining the sample size needed for a particular level of accuracy, and in selecting the sampling strategy best suited to your study.

#### Factors affecting the inferences drawn from a sample

The above principles suggest that two factors may influence the degree of certainty about the inferences drawn from a sample:

- 1. **The size of the sample** Findings based upon larger samples have more certainty than those based on smaller ones. As a rule, *the larger the sample size, the more accurate the findings*.
- 2. **The extent of variation in the sampling population** The greater the variation in the study population with respect to the characteristics under study, for a given sample size, the greater the uncertainty. (In technical terms, the greater the standard deviation, the higher the standard error for a given sample size in your estimates.) If a population is homogeneous (uniform or similar) with respect to the characteristics under study, a small sample can provide a reasonably good estimate, but if it is heterogeneous (dissimilar or diversified), you need to select a larger sample to obtain the same level of accuracy. Of course, if all the elements in a population are identical, then the selection of even one will provide an absolutely accurate estimate. As a rule, *the higher the variation with respect to the characteristics under study in the study population, the greater the uncertainty for a given sample size*.

## Aims in selecting a sample

When you select a sample in quantitative studies you are primarily aiming to achieve maximum precision in your estimates within a given sample size, and avoid bias in the selection of your sample.

Bias in the selection of a sample can occur if:

- sampling is done by a non-random method that is, if the selection is consciously or unconsciously influenced by human choice;
- the sampling frame list, index or other population records which serves as the basis of

selection, does not cover the sampling population accurately and completely;

• a section of a sampling population is impossible to find or refuses to co-operate.

# Types of sampling

The various sampling strategies in quantitative research can be categorised as follows (Figure 12.2):



FIGURE 12.2 Types of sampling in quantitative research

- random/probability sampling designs;
- non-random/non-probability sampling designs selecting a predetermined sample size;
- 'mixed' sampling design.

To understand these designs, we will discuss each type individually.

# Random/probability sampling designs

For a design to be called **random sampling** or **probability sampling**, it is imperative that each element in the population has an *equal* and *independent* chance of selection in the sample. Equal implies that the

probability of selection of each element in the population is the same; that is, the choice of an element in the sample is not influenced by other considerations such as personal preference. The concept of independence means that the choice of one element is not dependent upon the choice of another element in the sampling; that is, the selection or rejection of one element does not affect the inclusion or exclusion of another. To explain these concepts let us return to our example of the class.

Suppose there are 80 students in the class. Assume 20 of these refuse to participate in your study. You want the entire population of 80 students in your study but, as 20 refuse to participate, you can only use a sample of 60 students. The 20 students who refuse to participate could have strong feelings about the issues you wish to explore, but your findings will not reflect their opinions. Their exclusion from your study means that each of the 80 students does not have an equal chance of selection. Therefore, your sample does not represent the total class.

The same could apply to a community. In a community, in addition to the refusal to participate, let us assume that you are unable to identify all the residents living in the community. If a significant proportion of people cannot be included in the sampling population because they either cannot be identified or refuse to participate, then any sample drawn will not give each element in the sampling population an equal chance of being selected in the sample. Hence, the sample will not be representative of the total community.

To understand the concept of an *independent chance of selection*, let us assume that there are five students in the class who are extremely close friends. If one of them is selected but refuses to participate because the other four are not chosen, and you are therefore forced to select either the five or none, then your sample will not be considered an independent sample since the selection of one is dependent upon the selection of others. The same could happen in the community where a small group says that either all of them or none of them will participate in the study. In these situations where you are forced either to include or to exclude a part of the sampling population, the sample is not considered to be independent, and hence is not representative of the sampling population. However, if the number of refusals is fairly small, in practical terms, it should not make the sample non-representative. In practice there are always some people who do not want to participate in the study but you only need to worry if the number is significantly large.

A sample can only be considered a random/probability sample (and therefore representative of the population under study) if both these conditions are met. Otherwise, bias can be introduced into the study.

There are two main advantages of random/probability samples:

- 1. As they represent the total sampling population, the inferences drawn from such samples can be generalised to the total sampling population.
- 2. Some statistical tests based upon the theory of probability can be applied only to data collected from random samples. Some of these tests are important for establishing conclusive correlations.

#### Methods of drawing a random sample

Of the methods that you can adopt to select a random sample the three most common are:

1. **The fishbowl draw** – if your total population is small, an easy procedure is to number each element using separate slips of paper for each element, put all the slips into a box and then pick them out one by one without looking, until the number of slips selected equals the sample size you

decided upon. This method is used in some lotteries.

- 2. **Computer program** there are a number of programs that can help you to select a random sample.
- 3. **A table of randomly generated numbers** most books on research methodology and statistics include a table of randomly generated numbers in their appendices (see, e.g., Table 12.3). You can select your sample using these tables according to the procedure described in Figure 12.3.

The procedure for selecting a sample using a **table of random numbers** is as follows:

Let us take an example to illustrate the use of Table 12.3 for random numbers. Let us assume that your sampling population consists of 256 individuals. Number each individual from 1 to 256. Randomly select the starting page, set of column (1 to 10) or row from the table and then identify three columns or rows of numbers.

Suppose you identify the ninth column of numbers and the last three digits of this column (underlined). Assume that you are selecting 10 per cent of the total population as your sample (25 elements). Let us go through the numbers underlined in the ninth set of columns. The first number is 049 which is below 256 (total population); hence, the 49th element becomes a part of your sample. The second number, 319, is more than the total elements in your population (256); hence, you cannot accept the 319th element in the sample. The same applies to the next element, 758, and indeed the next five elements, 589, 507, 483, 487 and 540. After 540 is 232, and as this number is within the sampling frame, it can be accepted as a part of the sample. Similarly, if you follow down the same three digits in the same column, you select 052, 029, 065, 246 and 161, before you come to the element 029 again. As the 29th element has already been selected, go to the next number, and so on until 25 elements have been chosen. Once you have reached the end of a column, you can either move to the next set of columns or randomly select another one in order to continue the process of selection. For example, the 25 elements shown in Table 12.4 are selected from the ninth, tenth and second columns of Table 12.3.

TABLE 12.3Selecting a sample using a table for random numbers

	1	2	3	4	5	6	7	8	9	10
1	48461	14952	72619	73689	52059	37086	60050	86192	67049	64739
2	76534	38149	49692	31366	52093	15422	20498	33901	10319	43397
3	70437	25861	38504	14752	23757	29660	67844	78815	23758	86814
4	59584	03370	42806	11393	71722	93804	09095	07856	55589	46820
5	04285	58554	16085	51555	27501	73883	33427	33343	45507	50063
6	77340	10412	69189	85171	29802	44785	86368	02583	96483	76553
7	59183	62687	91778	80354	23512	97219	65921	02035	59487	91403
8	91800	04281	39979	03927	82564	28777	59049	97532	54540	79472
9	12066	24817	81099	48940	69554	55925	48379	12866	41232	21580
10	69907	91751	53512	23748	65906	91385	84983	27915	48491	91068
11	80467	04873	54053	25955	48518	13815	37707	68687	15570	08890
12	78057	67835	28302	45048	56761	97725	58438	91529	24645	18544
13	05648	39387	78191	88415	60269	94880	58812	42931	71898	61534
14	22304	39246	01350	99451	61862	78688	30339	60222	74052	25740
15	61346	50269	67005	40442	33100	16742	61640	21046	31909	72641
16	56793	37696	27965	30459	91011	51426	31006	77468	61029	57108
17	56411	48609	36698	42453	85061	43769	39948	87031	30767	13953
18	62098	12825	81744	28882	27369	88185	65846	92545	09065	22653
19	68775	06261	54265	16203	23340	84750	16317	88686	86842	00879
20	52679	19599	13687	74872	89181	01939	18447	10787	76246	80072
21	84096	87152	20719	25215	04349	54434	72344	93008	83282	31670
22	83964	55937	21417	49944	38356	98404	14850	17994	17161	98981
23	31191	75131	72386	11689	95727	05414	88727	45583	22568	77700
24	30545	68523	29850	67833	05622	89975	79042	27142	99257	32349
25	52573	91001	52315	26430	54175	30122	31796	98842	37600	26025
26	16586	81842	01076	99414	31574	94719	34656	80018	86988	79234
27	81841	88481	61191	25013	30272	23388	22463	65774	10029	58376
28	43563	66829	72838	08074	57080	15446	11034	98143	74989	26885
29	19945	84193	57581	77252	85604	45412	43556	27518	90572	00563
30	79374	23796	16919	99691	80276	32818	62953	78831	54395	30705
31	48503	26615	43980	09810	38289	66679	73799	48418	12647	40044
32	32049	65541	37937	41105	70106	89706	40829	40789	59547	00783
33	18547	71562	95493	34112	76895	46766	96395	31718	48302	45893
34	03180	96742	61486	43305	84183	99605	67803	13491	09243	29557
35	94822	24738	67749	83748	59799	25210	31093	62925	72061	69991
36	04330	60599	85828	19152	68499	27977	35611	96240	62747	89529
37	43770	81537	59527	95674	76692	86420	69930	10020	72881	12532
38	56908	77192	50623	41215	14311	42834	80651	93750	59957	31211
39	32787	07189	80539	75927	75475	73965	11796	72140	48944	74156
40	52441	78392	11733	57703	29133	71164	55355	31006	25526	55790
41	22377	54723	18227	28449	04570	18882	00023	67101	06895	08915
42	18376	73460	88841	39602	34049	20589	05701	08249	74213	25220
43	53201	28610	87957	21497	64729	64983	71551	99016	87903	63875
44	34919	78801	59710	27396	02593	05665	11964	44134	00273	76358
45	33617	92159	21971	16901	57383	34262	41744	60891	57624	06962
46	70010	40964	98780	72418	52571	18415	64362	90637	38034	04909
47	19282	68447	35665	31530	59838	49181	21914	65742	89815	39231
48	91429	73328	13266	54898	68795	40948	80808	63887	89939	47938
49	97637	78393	33021	05867	86520	45363	43066	00988	64040	09803
50	95150	07625	05255	83254	93943	52325	93230	62668	79529	66964

*Source: Statistical Tables*, 3e, by F. James Rohlf and Robert R. Sokal. Copyright © 1969, 1981, 1994 by W.H. Freeman and Company. Used with permission.

Step 1	Identify the total number of elements in the study population, for example 50, 100, 430, 795 or 1265. The total number of elements in a study population may run up to four or more digits (if your total sampling population is 9 or less, it is one digit; if it is 99 or less, it is two digits;).
Step 2	Number each element starting from 1.
Step 3	If the table for random numbers is on more than one page, choose the starting page by a random procedure. Again, select a column or row that will be your starting point with a random procedure and proceed from there in a predetermined direction.
Step 4	Corresponding to the number of digits to which the total population runs, select the same number, randomly, of columns or rows of digits from the table.
Step 5	Decide on your sample size.
Step 6	Select the required number of elements for your sample from the table. If you happen to select the same number twice, discard it and go to the next. This can happen as the table for random numbers is generated by sampling with replacement.

FIGURE 12.3 The procedure for using a table of random numbers

TABLE 12.4	Selected e	elements	using	the	table	of	randor	n nun	ibers
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Column in Table 12.3		Ele			
9	49 246 34	232 161 40	52 243	29 61	65 213
10	63 234 231	68 44	108 211	72 156	25 220
2	149	246			